




**Understanding EMC Basics series**  
**Webinar #1 of 3, February 27, 2013**  
**EM field theory, and 3 types of EM analysis**




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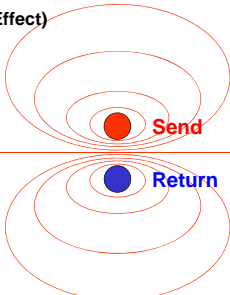
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**Contents of Webinar #1**

1. Electromagnetic fields, waves, and the importance of the return current path
2. Field theory, permittivity, permeability, wave impedance and velocity
3. Near-field and Far-field
4. Three types of EMC analysis (includes Skin Effect)



**Understanding EMC Basics**

**1**

**Electromagnetic fields and waves, and the importance of the return current path**

**Electromagnetic (EM) fields**

- Every non-DC voltage/current is a wave of propagating EM energy...
  - guided by send and return current paths
    - and the insulators (dielectrics) that surround them (e.g. air)
- EM waves spread out and create EM fields, (like ripples spreading out and making a pattern on a pool)...
  - and we measure fields in terms of field strength
- Design for EMC is mostly about controlling fields
  - so that they are *high* where we *want* power or signals
  - and *low* where we *don't want* emissions or susceptibility

**Of course, a wave has different amplitudes along its path**

- When a conductor is long enough
  - it *cannot* experience the same voltage or current, at the same time, over its whole length...
    - which is why high frequencies seem to behave so weirdly!
- The ratio between wavelength ( $\lambda$ ) and conductor dimension is very important
  - we can usually ignore “wave effects” when the dimension we are concerned with is  $< 1/100^{\text{th}}$  of the  $\lambda$ ...
    - e.g. at 1GHz:
      - $< 3\text{mm}$  in air ( $\lambda = 300\text{mm}$ );  $< 1.5\text{mm}$  in FR4 ( $\lambda = 150\text{mm}$ )



### Importance of the return current path

- Electric and magnetic fields are the *true nature* of electrical and electronic power and signals
  - and they both depend on the physical routes taken by the send and return currents
- A great deal of EMC design depends on controlling the paths of the return currents
- All currents always flow in complete loops...
  - taking the path of least impedance – the path with the least area – i.e. the return current flows as close to its send path as it is allowed to

## Understanding EMC Basics

# 2

## Field theory, permittivity, permeability, wave impedance and velocity

### We don't need field theory – just a few concepts

- Fluctuating voltages create Electric fields (E)
  - which are measured in Volts/metre (V/m)
- Fluctuating currents create Magnetic fields (H)
  - which are measured in Amps/metre (A/m)
- EM waves have power (P)
  - measured in Watts/square metre (W/m<sup>2</sup>)  
(i.e. the rate at which energy passes through an area)

### Permeability ( $\mu$ ) and permittivity ( $\epsilon$ )

- All media or materials have conductivity/resistivity (i.e. loss of EM energy, turned into heat),  $\mu$  and  $\epsilon$ ...
  - in vacuum (and air):  $\mu_0 = 4\pi \cdot 10^{-7}$  Henrys/metre...
    - i.e. the vacuum can contain magnetic field energy
  - And:  $\epsilon_0 = (1/36\pi) \cdot 10^{-9}$  Farads/metre
    - i.e. the vacuum can also contain electric field energy
- Other media and materials are characterised by their *relative* permeability ( $\mu_R$ ) and permittivity ( $\epsilon_R$ )
  - so their *absolute* permeability is:  $\mu_0\mu_R$   
and their *absolute* permittivity is:  $\epsilon_0\epsilon_R$

### Permeability ( $\mu$ ) and permittivity ( $\epsilon$ ) continued...

- In conductors (e.g. wires, PCB traces):  $\mu$  and  $\epsilon$  are what causes them to have inductance (L) and capacitance (C)...
  - so *whenever* there is a fluctuating *voltage* (V) there is *always* an associated *current* (I), and vice-versa
- In insulators (e.g. PVC, FR4, air):  $\mu$  and  $\epsilon$  cause effects *similar to* inductance and capacitance...
  - so *whenever* there is a fluctuating *electric field* (E) there is *always* an associated *magnetic field* (H), and vice-versa

### $\mu$ and $\epsilon$ govern an EM wave's impedance, and it's propagation velocity

- For the wave's 'far field' impedance ...
 
$$Z = E/H = V/m \div A/m = \sqrt{(\mu_0\mu_R/\epsilon_0\epsilon_R)} \Omega$$

$$Z = 377\Omega \quad \text{in air or vacuum}$$

$$Z = 377\sqrt{(\mu_R/\epsilon_R)} \quad \text{in a medium or material}$$
- For the velocity of the wave's propagation ...
 
$$v = 1/\sqrt{(\mu_0\mu_R\epsilon_0\epsilon_R)} \quad \text{metres/second}$$

$$v = 3.10^8 \text{ m/s in air or vacuum (i.e. the speed of light)}$$

$$v = 3.10^8/\sqrt{(\mu_R\epsilon_R)} \text{ m/s in a medium or material}$$

**And the velocity of wave propagation ( $v$ ) links frequency ( $f$ ) to wavelength ( $\lambda$ )**

$$v = f \lambda$$

- In vacuum or air:  $v = c = 300$  million metres/second
  - $1/\sqrt{(\mu_0 \epsilon_0)}$ , equivalent to 3ns/metre, 3ps/millimetre
- But in media or materials with  $\mu_R$  and/or  $\epsilon_R > 1.0$ ,  $v$  is *slower* than  $c$ 
  - so the wavelength ( $\lambda$ ) is shorter (for a given  $f$ )
    - e.g. for a printed-circuit board trace,  $v$  is approx. 50% of  $c$
    - ....so a  $\lambda$  is approx. 50% of what it would be in air

**Understanding EMC Basics**

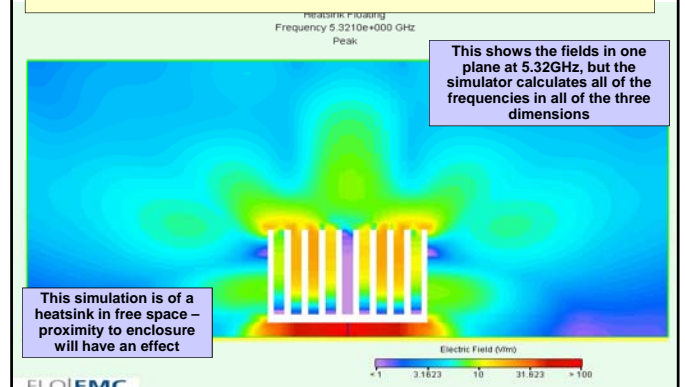
**3**

**Near Field and Far Field**

**Near-field and Far-field**

- Near fluctuating voltages or currents, E and H fields have complex patterns: field strengths vary as  $1/r^3$ ,  $1/r^2$  and  $1/r$ 
  - where  $r$  is the radial distance from the source
  - because of stray capacitance and stray mutual inductance effects (i.e. E and H field coupling)
- But, far enough away, the fields become EM waves (E and H fields in the ratio of the wave impedance:  $Z$ )...
  - and have simple ‘plane wave’ spherical distributions with field strengths that vary as  $1/r$

**An example of a near-field field distribution**



**Near-field and Far-field continued...**

- For sources with longest dimensions  $\ll \lambda$ , the boundary between the near and far field regions is:

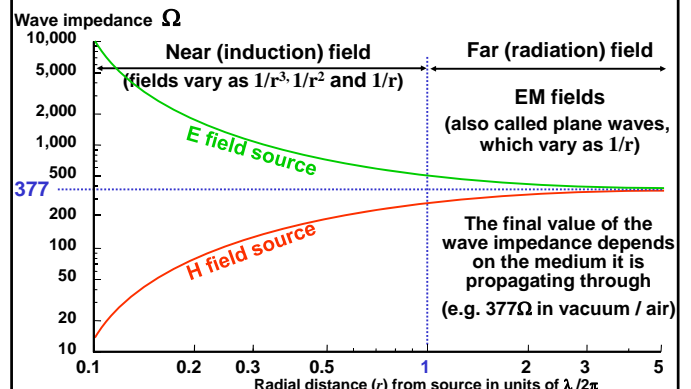
$$r = \lambda/2\pi$$

- But for sources with dimensions  $> \lambda$ , the near/far field boundary is:

$$r = 2D^2/\lambda$$

– where  $D$  is the largest dimension of the source

**Near-field and far-field when the source's largest dimension is  $\ll \lambda$  (for illustration only)**



## Poll Questions

## Understanding EMC Basics

### 4

#### Three types of EMC analysis (includes Skin Effect)

### EMC uses three types of analysis

- For conductor dimensions  $< \lambda/6$  we can use '**lumped circuit analysis**' methods (based on R, L, C)
- When conductor dimension is  $> \lambda/6$  along one axis (e.g. a wire) we must use '**transmission line**' analysis
- But when conductors are  $> \lambda/6$  in two or three dimensions we must use '**full-wave analysis**'
  - based on Maxwell's Equations
    - only practical for very simple situations, or when using computers to do the analysis

### Resonances

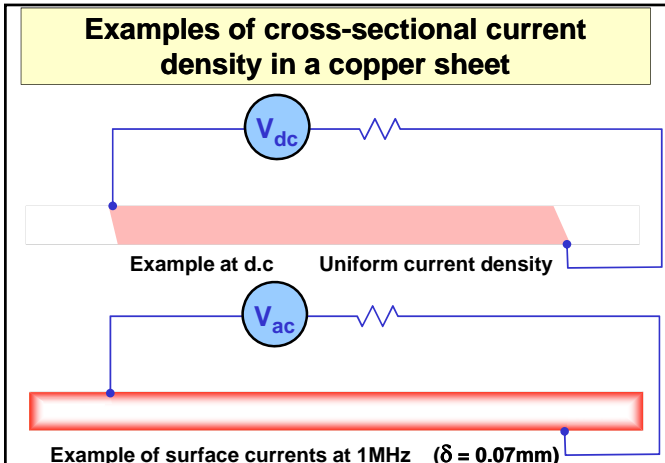
- **All** circuits have RF resonant modes
  - where their currents or voltages experience resonant gain, called their 'Q factor'...
  - Qs of 100 or more are common (i.e. gains of 40dB or more)
- As the voltage peaks, the current nulls, and vice-versa (to maintain a constant energy as the wave propagates)
- High levels of emissions (and poor immunity) tend to occur at resonances...
  - so we often need to control them to achieve EMC

### Lumped analysis... **everything** has resistance (R), inductance (L), and capacitance (C)

- including all components, wires, cables, PCB tracks, connectors, silicon metallisation, bond wires, etc
- also including their 'stray' or 'parasitic' Rs, Ls, and Cs
  - which can be intrinsic (e.g. the self-inductance of a wire lead)
  - or extrinsic (e.g. stray C or L coupling due to proximity to other objects)
- Resistance increases with  $f$  due to Skin Effect

### Lumped analysis: Resistance and Skin Effect

- DC currents travel through the *whole* cross-sectional area of a conductor
  - but AC currents are forced to flow close to the surface
- This is known as the "skin effect"
- So, high-frequency currents only penetrate weakly into the *depth* (thickness) of a conductor
  - increasing the resistance in their path

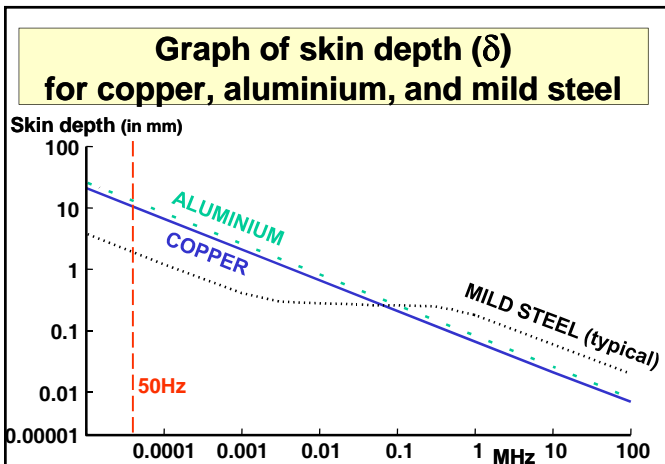


### Resistance and Skin effect      continued...

- One skin depth ( $\delta$ ) is the depth into the conductor by which the current density has reduced to  $1/e$

$$\delta = \frac{1}{\sqrt{(\pi f \mu_0 \mu_R \sigma)}} \text{ metres}$$

- where  $\sigma$  = conductivity
- For copper conductors:  $\delta = 66/\sqrt{f}$   
( $f$  in Hz gives  $\delta$  in millimetres)
- e.g. at 160MHz  $\delta = 0.005\text{mm}$ , so 0.05mm below the surface (10 skin depths) the current density is negligible



### Lumped analysis: Stray Inductance

- E.g. a thin wire has self-inductance of about  $1\mu\text{H}$  per metre ( $1\text{nH}$  per mm)
  - this assumes its return current path is very far away
  - a close return path reduces the overall inductance experienced by the send/return current
- Close proximity to ferromagnetic materials (e.g. steel) with  $\mu_r > 1$  will *increase* its self-inductance
- But close proximity to conductors (e.g. cables, metalwork, etc.) will *decrease* self-inductance

### Lumped analysis: Stray Capacitance

- E.g. a thin wire on its own in free space has about  $40\text{pF}$  per metre length (approx.  $0.04\text{pF}$  per mm)....
  - this is its ‘space charge’ capacitance....
  - close proximity to dielectrics ( $\epsilon_r > 1$ ) will add more stray space charge capacitance
- Proximity of conductors adds stray capacitance...
  - $(8.8/d)$  nF/square metre in air ( $d$  is the spacing in mm)
  - $(8.8 \epsilon_r/d)$  nF/sq. m., when  $d$  is the spacing through insulation

### Lumped Analysis: Resonances

- L and C store energy in their E and H fields
  - this is true for intentional Ls and Cs (e.g. components) and ‘stray’ or ‘parasitic’ Ls and Cs
- All types of circuits have L and C (even if they are only strays) and these cause resonances, at:  
 $f_{\text{RES}} = 1/(2\pi\sqrt{LC})$
- These resonances are ‘damped’ by the resistances in the circuit

**Transmission line analysis...**  
all send/return conductors have  
*characteristic impedance* (called  $Z_0$ )

- The  $L$  and  $C$  associated with a small length governs the velocity ( $v$ ) with which EM waves travel through that length...  $v = 1/\sqrt{LC}$
- And the ratio of the  $L$  to the  $C$  governs the characteristic impedance ( $Z_0$ ) of that length...  
 $Z_0 = \sqrt{L/C}$
- Note: the  $L$  and  $C$  values used in the above expressions are 'per unit length' (e.g.  $1\mu\text{H}/\text{metre}$ ,  $100\text{pF}/\text{metre}$ ) where the unit lengths used are shorter than  $\lambda/6$

**The effects of keeping  $Z_0$  constant**

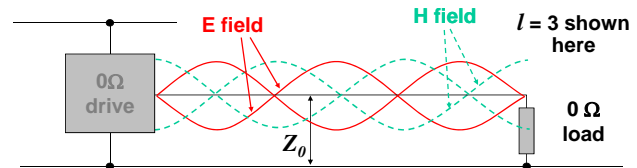
- If  $Z_0$  is kept constant from source to load, almost 100% of the wave (= signal) is communicated
  - which means that there must be **low emissions** from the wanted signal (because there is very little energy lost)
- This is called *matched transmission line* design
  - and a matched transmission line is a very inefficient antenna
    - which is why all general purpose RF test equipment has  $50\Omega$  inputs and outputs, connected with '50 $\Omega$  cable'

**Changes in  $Z_0$**   
over dimensions greater than  $\lambda/6$

- These cause propagating EM waves to be reflected (whether they are signals or power)
  - like the ripples spreading in a pool of water reflecting from a floating stick
- The technique called "EMC filtering" relies upon creating changes in characteristic impedance
  - to reflect unwanted noise away from a protected circuit

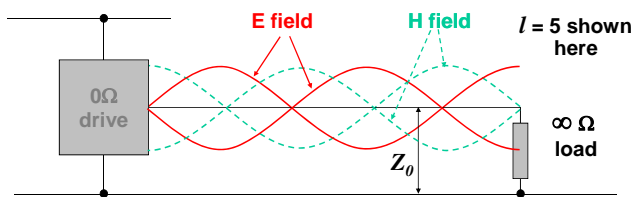
**Transmission-line analysis: Resonances**

- When a conductor has the same type of  $Z_0$  discontinuity at each end (whether the source and load impedances are both too high, or too low)...
  - resonances occur when conductor length is a whole number of half-wavelengths...  $f_{\text{res}} = 150 l/L$  (air dielectric) where  $l$  is an integer (1, 2, 3, etc.),  $L$  is conductor length (metres) and  $f_{\text{res}}$  is in MHz



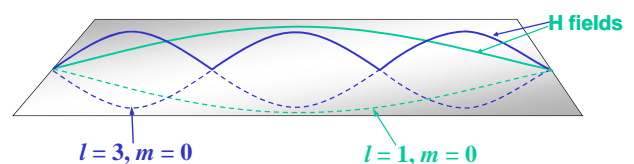
**Transmission-line analysis: Resonances**  
continued...

- When a conductor has opposing types of  $Z_0$  discontinuity at its ends...
  - resonances occur when conductor length is an odd number of quarter-wavelengths...  $f_{\text{res}} = 75 l/L$  (air dielectric) where  $l$  is an odd-numbered integer (1, 3, 5, etc.),  $L$  is conductor length (metres) and  $f_{\text{res}}$  is in MHz



**2-dimensional structural resonances:**  
**'standing waves' caused by reflections**  
**at the edges of a metal plate**

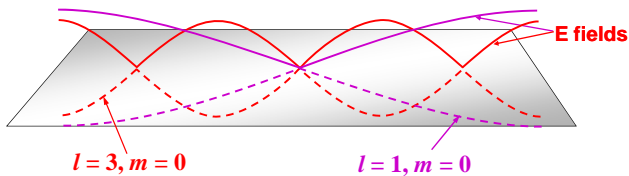
- Resonances can only occur at integer multiples of half-wavelengths, at:  
 $f_{\text{res}} = 150 \sqrt{\{(l/L)^2 + (m/W)^2\}}$  (in MHz)
  - where:  $l$  and  $m$  are integers (0, 1, 2, 3, etc.) and  $L$  and  $W$  are the plate's length and width (in metres)





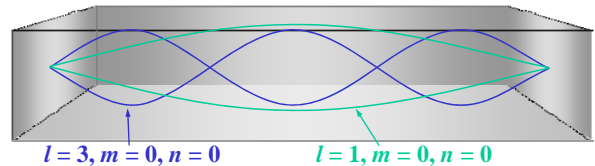
**'Standing waves' caused by reflections at the edges of a metal plate continued...**

- Magnetic field standing waves must have minima at the edges of the metal plate (air has much higher impedance than metal)...
  - whilst electric fields must be a maximum at the edges



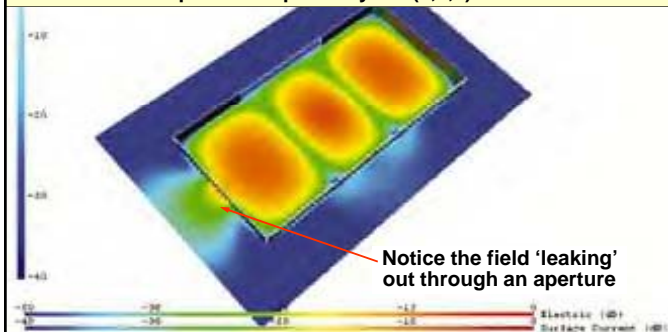
**3-dimensional structural resonances: 'standing waves' caused by reflections at the walls inside a metal box**

- Resonances can only occur at integer multiples of half-wavelengths, at:
 
$$f_{res} = 150 \sqrt{\{(l/L)^2 + (m/W)^2 + (n/H)^2\}} \text{ (in MHz)}$$
  - where:  $l, m, n$  are integers (0, 1, 2, 3, etc.)
  - and  $L, W, H$  are the box's length, width, height (in metres)



**A FLO/EMC simulation of the electric field distribution inside a shielded box**

The simulator calculates all frequencies, in three dimensions. This figure shows a 'slice' through a box at one of its resonant frequencies - probably the (3,0,0) mode



**Poll Questions**

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**the end**

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